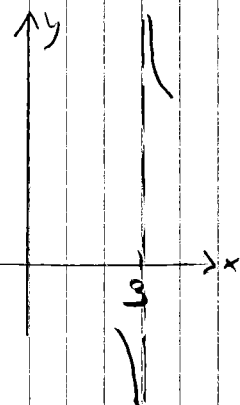


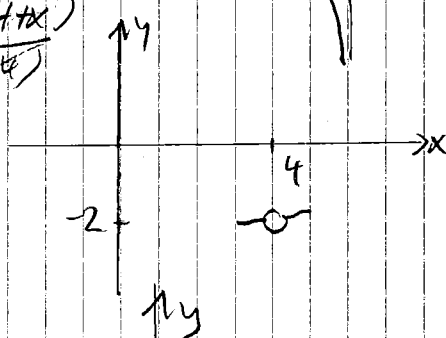
Math 3N corrigé exercices de préparation oral

Ex 1:

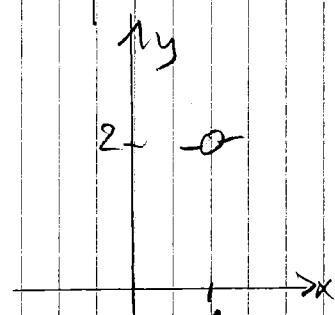
(a) type $\frac{\infty}{0}$ $\lim_{x \rightarrow 3^-} \frac{x^2 - 9}{3 - x} = \frac{-9}{0^+} = -\infty$
 $\lim_{x \rightarrow 3^+} \frac{x^2 - 9}{3 - x} = \frac{9}{0^-} = +\infty$ $\left. \begin{array}{l} \lim_{x \rightarrow 3} f(x) \text{ does not exist} \end{array} \right\}$



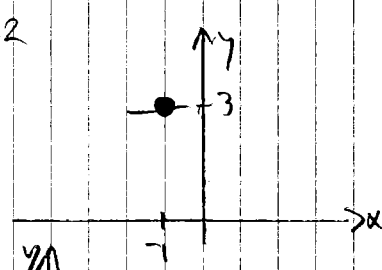
(b) type $\frac{0}{0}$ $\lim_{x \rightarrow 4} \frac{(4-x)(4+x)}{x(x-4)} = \lim_{x \rightarrow 4} \frac{-(x-4)(4+x)}{x(x-4)}$
 $= -\frac{8}{4} = -2$



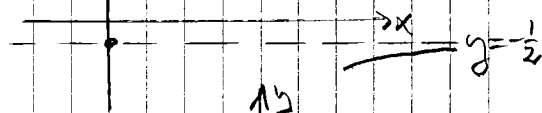
(c) type $\frac{0}{0}$ $\lim_{x \rightarrow 1} \frac{(x-1)(3+\sqrt{12-3x})}{(3-\sqrt{12-3x})(3+\sqrt{12-3x})}$
 $= \lim_{x \rightarrow 1} \frac{(x-1)(3+\sqrt{12-3x})}{9 - (12-3x)}$
 $= \lim_{x \rightarrow 1} \frac{(x-1)(3+\sqrt{12-3x})}{-3+3x}$
 $= \lim_{x \rightarrow 1} \frac{(x-1)(3+\sqrt{12-3x})}{3(x-1)} = \frac{6}{3} = 2$



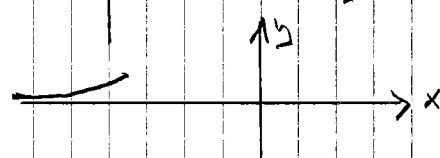
(d) direct $\lim_{x \rightarrow -1} f(x) = \frac{\sqrt{4+4}}{2} = 3$



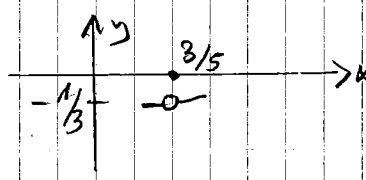
(e) type $\frac{\infty}{\infty}$ $\lim_{x \rightarrow \infty} \frac{x^3(-1 + 1/x^2)}{x^3(2 + 1/x^3)} = -\frac{1}{2}$



(f) direct $\lim_{x \rightarrow -\infty} f(x) = \frac{-8}{1-4(-\infty)^2} = \frac{-8}{+\infty} = 0$



(g) type $\frac{0}{0}$ $\lim_{x \rightarrow 3/5} \frac{\sin(3-5x)}{-3(3-5x)} = -\frac{1}{3} \lim_{3-5x \rightarrow 0} \frac{\sin(3-5x)}{3-5x} = -\frac{1}{3} \cdot 1 = -\frac{1}{3}$
 $5x \rightarrow 3$
 $5x - 3 \rightarrow 0$
 $-5x + 3 \rightarrow 0$
 $3 - 5x \rightarrow 0$



as vert: candidats $x=1$ et $x=-1$
 $\left. \begin{array}{l} \text{type } \frac{0}{0} \\ \rightarrow \text{as. vert} \end{array} \right\} \begin{array}{l} \text{type } \frac{0}{0} \\ \rightarrow \text{à voir...} \end{array}$

$$\lim_{x \rightarrow -1} f(x) = \lim_{x \rightarrow -1} \frac{3x^2(x+1)}{2(1-x)(1+x)} = \frac{3}{-2 \cdot 2} = -\frac{3}{4} \text{ pas d'as. vert}$$

$$\left. \begin{array}{l} \lim_{x \rightarrow 1^-} f(x) = \frac{6}{-2 \cdot 0^+ \cdot 2} = -\infty \\ \lim_{x \rightarrow 1^+} f(x) = \frac{6}{-2 \cdot 0^- \cdot 2} = +\infty \end{array} \right\} x=1 \text{ as. vert de } f$$

Ex 3 :

$$\begin{aligned} \left(\frac{3x^3 + 3x^2}{2 - 2x^2} \right)' &= \frac{(9x^2 + 6x)(2 - 2x^2) - (3x^3 + 3x^2)(-4x)}{(2 - 2x^2)^2} \\ &= \frac{3x(3x+2) \cdot 2(1-x)(1+x) + 3x^2(x+1) \cdot 4x}{[2(1-x^2)]^2} \\ &= \frac{3x(x+1) \cdot 2[(3x+2)(1-x) + 2x^2]}{2^4(1-x)^2(1+x)^2} \\ &= \frac{3x(x+1)[3x+2-3x^2-2x+2x^2]}{2(1-x)^2(1+x)^2} = \frac{3x(x+1)(-x^2+x+2)}{2(1-x)^2(1+x)^2} \\ &= \frac{3x(x+1)(-1)(x^2-x-2)}{2(1-x)^2(1+x)^2} = \frac{-3x(x+1)(x-2)(x+1)}{2(x-1)^2(x+1)^2} \stackrel{x \neq -1}{=} \frac{-3x(x-2)}{2(x-1)^2} \end{aligned}$$

remarque: on peut être plus malin

$$f(x) = \frac{3x^2(x+1)}{2(1-x)(1+x)} \stackrel{x \neq -1}{=} \frac{3x^2}{2(1-x)} \quad \text{on simplifie avec le dénominateur!}$$

$$\begin{aligned} \Rightarrow f'(x) &= \left[\frac{3x^2}{2(1-x)} \right]' = \frac{6x(1-x) - 3x^2(-1)}{[2(1-x)]^2} \\ &= \frac{+12x(1-x) + 6x^2}{4(1-x)^2} = \frac{+12x + 12x^2 + 6x^2}{4(1-x)^2} = \frac{-6x^2 + 12x}{4(1-x)^2} \\ &= \frac{-6x(x-2)}{4(1-x)^2} = \frac{-3x(x-2)}{2(1-x)^2} \end{aligned}$$

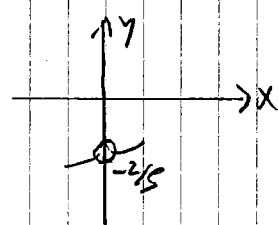
(h) direct

$$\lim_{x \rightarrow 7} f(x) = \frac{\sin(0)}{\cos(0)} = \frac{0}{1} = 0$$



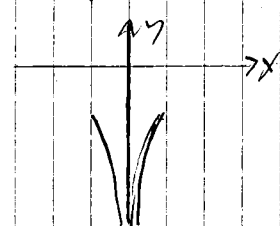
(i) type $\frac{0}{0}$
l'Hôpital

$$\begin{aligned} \lim_{x \rightarrow 0} \frac{\sin(-2x)}{\cos(-2x)} \cdot \frac{1}{5x} &= \lim_{x \rightarrow 0} \frac{1(-2) \sin(-2x)}{-2x} \cdot \frac{1}{\cos(-2x)} \\ &= -\frac{2}{5} \lim_{-2x \rightarrow 0} \frac{\sin(-2x)}{-2x} \lim_{x \rightarrow 0} \frac{1}{\cos(-2x)} \\ &= -\frac{2}{5} \cdot 1 \cdot \frac{1}{\cos(0)} = -\frac{2}{5} \end{aligned}$$



(j) type $\frac{\infty}{0}$

$$\begin{aligned} \lim_{x \rightarrow 0^+} f(x) &= \frac{4 \cdot 1}{-2 \cdot 0^+} = -\infty \\ \lim_{x \rightarrow 0^-} f(x) &= \frac{4}{-2 \cdot 0^+} = -\infty \end{aligned} \quad \left. \vphantom{\lim_{x \rightarrow 0^+} f(x)} \right\} \lim_{x \rightarrow 0} f(x) = -\infty$$



Ex 2: $f(x) = \frac{3x^3 + 3x^2}{2 - 2x^2} = \frac{3x^2(x+1)}{-2(1-x)(1+x)}$

• as. horizont? non car $d^0(\text{num}) > d^0(\text{denom})$

verif: $\lim_{x \rightarrow \pm\infty} \frac{x^3(3 + 3/x)}{x^2(-2 - 2/x^2)} = \pm\infty$ par d'as. horizont.

• as. oblique?

méthode 1: $a = \lim_{x \rightarrow \pm\infty} \frac{f(x)}{x} = \lim_{x \rightarrow \pm\infty} \frac{3x^3 + 3x^2}{2x - 2x^3} = \lim_{x \rightarrow \pm\infty} \frac{x^2(3 + 3/x)}{x^2(-2 + 2/x^2)} = -\frac{3}{2}$

$$\begin{aligned} b &= \lim_{x \rightarrow \pm\infty} f(x) - ax = \lim_{x \rightarrow \pm\infty} \frac{3x^3 + 3x^2}{2 - 2x^2} + \frac{3x}{2} = \lim_{x \rightarrow \pm\infty} \frac{3x^3 + 3x^2 + 6x - 6x^2}{2 - 2x^2} \\ &= \lim_{x \rightarrow \pm\infty} \frac{x^2(3 + 6/x)}{x^2(-2 + 2/x^2)} = -\frac{3}{2} \end{aligned}$$

d'où $y = -\frac{3}{2}x - \frac{3}{2}$ as. oblique de f à $\pm\infty$

méthode 2:

$$\begin{array}{r|l} 3x^3 + 3x^2 & -2x^2 + 2 \\ - (3x^3 - 3x) & -\frac{3}{2}x - \frac{3}{2} \\ \hline 3x^2 + 3x & \\ - (3x^2 - 3) & \\ \hline 3x + 3 & \end{array}$$

d'où $(3x^3 + 3x^2) = (-2x^2 + 2)(-\frac{3}{2}x - \frac{3}{2}) + (3x + 3)$

et $f(x) = (-\frac{3}{2}x - \frac{3}{2}) + \frac{3x + 3}{-2x^2 + 2}$

donc $\lim_{x \rightarrow \pm\infty} f(x) = (-\frac{3}{2}x - \frac{3}{2}) + \lim_{x \rightarrow \pm\infty} \frac{3x + 3}{-2x^2 + 2} = -\infty$

et d'où $y = -\frac{3}{2}x - \frac{3}{2}$ as. oblique de f à $\pm\infty$

x		0		1		2	
-3x	+	0	-	-	-	-	-
x-2	-	-	-	-	-	0	+
2(1-x) ²	+	+	+	0	+	+	+
f'(x)	-	0	+	0	+	0	-
f(x)	↘	m	↗	↗	↗	m	↘

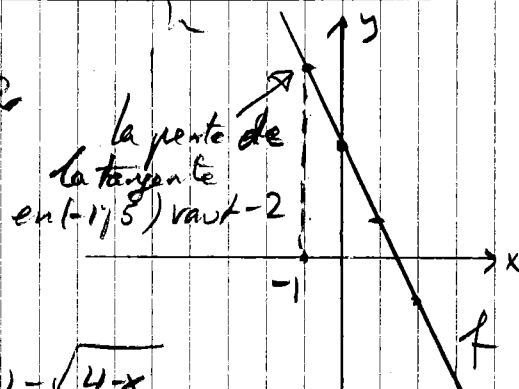
f admet un maximum en $x=0$; il vaut $f(0)=0$

" " " maximum en $x=2$; il vaut $f(2) = \frac{3 \cdot 8 + 3 \cdot 4}{2 \cdot 2 \cdot 4} = \frac{36}{8} = 4.5$

Ex 4

$$(a) f'(-1) = \lim_{h \rightarrow 0} \frac{f(-1+h) - f(-1)}{h} = \lim_{h \rightarrow 0} \frac{[-2(-1+h)+3] - [-2(-1)+3]}{h}$$

$$= \lim_{h \rightarrow 0} \frac{2-2h+3-5}{h} = \lim_{h \rightarrow 0} \frac{-2h}{h} = -2$$



$$(b) f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \rightarrow 0} \frac{\sqrt{4-(x+h)} - \sqrt{4-x}}{h}$$

$$= \lim_{h \rightarrow 0} \frac{[\sqrt{4-x-h} - \sqrt{4-x}][\sqrt{4-x-h} + \sqrt{4-x}]}{h[\sqrt{4-x-h} + \sqrt{4-x}]}$$

$$= \lim_{h \rightarrow 0} \frac{(4-x-h) - (4-x)}{h[\sqrt{4-x-h} + \sqrt{4-x}]} = \lim_{h \rightarrow 0} \frac{-h}{h[\sqrt{4-x-h} + \sqrt{4-x}]}$$

$$= \frac{-1}{\sqrt{4-x+0} + \sqrt{4-x}} = \frac{-1}{2\sqrt{4-x}}$$

Ex 5

$$a) f'(x) = 2\left(\frac{1}{x}\right)' + (x^{1/3})' - (56)' = 2\left(-\frac{1}{x^2}\right) + \frac{1}{3}x^{-2/3} - 0 \\ = -\frac{2}{x^2} + \frac{1}{3\sqrt[3]{x^2}}$$

$$b) f'(x) = \frac{(6x-2)(x-1) - (3x^2-2x+2)}{(x-1)^2}$$

$$c) f'(x) = -4[(x^2+1)^{1/2}]' = -4 \cdot \frac{1}{2}(x^2+1)^{-1/2} \cdot (x^2+1)' = -2 \cdot \frac{2x}{\sqrt{x^2+1}}$$

$$d) f'(x) = 9(4-3x)^8 \cdot (-3)(2x^2+1)' + (4-3x)^9 \cdot 6(2x^2+1)^5 \cdot 4x \\ = 3(4-3x)^8(2x^2+1)^5 [-9(2x^2+1) + 8x(4-3x)] \\ = 3(4-3x)^8(2x^2+1)^5 [-18x^2-9+32x-24x^2] \\ = 3(4-3x)^8(2x^2+1)^5 [-42x^2+32x+9] \\ \Delta < 0 \text{ non factorisable}$$

$$e) f'(x) = \cos(-x)(-1) + 1 + \tan^2(x) = -\cos(-x) + 1 + \tan^2(x)$$

$$f) g'(x) = -\sin(x^5+x) \cdot (5x^4+1)$$

$$g) f'(x) = \left(\cos\left(\frac{1}{4x+1}\right)\right)^{10}' = 10 \cos^9\left(\frac{1}{4x+1}\right) \cdot \left[\cos\left(\frac{1}{4x+1}\right)\right]' \\ = 10 \cos^9\left(\frac{1}{4x+1}\right) \cdot \left(-\sin\left(\frac{1}{4x+1}\right)\right) \cdot \frac{-4}{(4x+1)^2} \\ = 40 \cos^9\left(\frac{1}{4x+1}\right) \sin\left(\frac{1}{4x+1}\right) \cdot \frac{1}{(4x+1)^2}$$

$$h) f'(x) = 3x^2 - [1 \cdot \sqrt{2x} + x \cdot [(2x)^{1/2}]'] \\ = 3x^2 - \sqrt{2x} - x - \frac{1}{2}(2x)^{-1/2} \cdot (2x)' \\ = 3x^2 - \sqrt{2x} - \frac{x}{2\sqrt{2x}} \cdot 2 = 3x^2 - \sqrt{2x} - \frac{x}{\sqrt{2x}}$$

$$i) f'(x) = [1 + \lg^2(\sin(x))] \cdot \cos(x)$$

ex 6

$$(a) \left(\frac{1}{2x-1} \right)' = - \frac{(2x-1)'}{(2x-1)^2} = - \frac{2}{(2x-1)^2}$$

$$(b) f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \rightarrow 0} \frac{\frac{1}{2(x+h)-1} - \frac{1}{2x-1}}{h} = \lim_{h \rightarrow 0} \frac{\frac{(2x-1) - [2(x+h)-1]}{[2(x+h)-1][2x-1]}}{h}$$

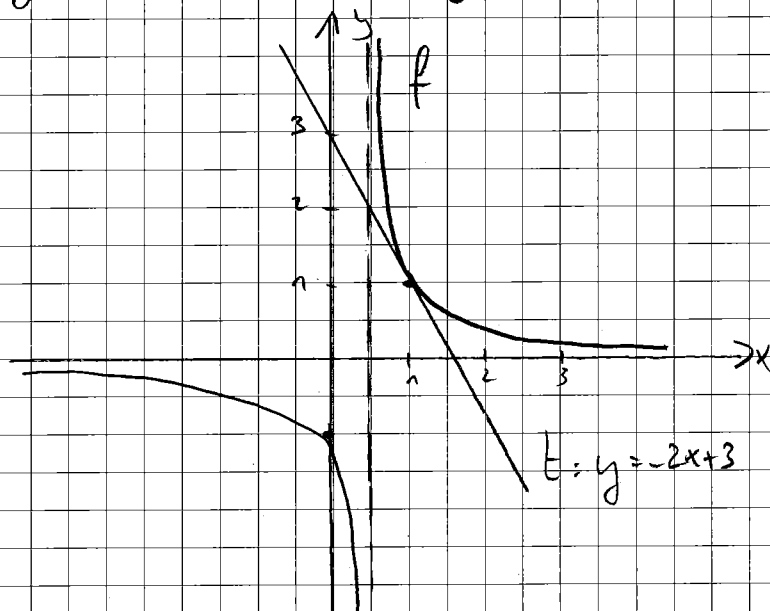
$$= \lim_{h \rightarrow 0} \frac{\cancel{2x} - \cancel{2x} - 2h + \cancel{1}}{[2(x+h)-1][2x-1] \cdot h} = \lim_{h \rightarrow 0} \frac{-2\cancel{h}}{[\dots][\dots]\cancel{h}} = \lim_{h \rightarrow 0} \frac{-2}{[2(x+h)-1][2x-1]}$$

$$= \frac{-2}{[2(x+0)-1][2x-1]} = \frac{-2}{(2x-1)^2}$$

$$(c) y = f'(1)(x-1) + f(1) \quad : \text{formule de l'eq. de la tg}$$

$$\Leftrightarrow y = \frac{-2}{(2 \cdot 1 - 1)^2} (x-1) + \frac{1}{2 \cdot 1 - 1}$$

$$\Leftrightarrow y = -2(x-1) + 1 \quad \Leftrightarrow y = -2x + 3$$



ex 7

$$(a) f'(x) = 12 \Leftrightarrow 3x^2 - 6x - 60 = 12 \Leftrightarrow 3x^2 - 6x - 72 = 0$$

$$(b) \Leftrightarrow 3(x^2 - 2x - 24) = 0 \Leftrightarrow 3(x-12)(x+2) = 0$$

$$x=12 \text{ ou } x=-2$$

$$1^{\text{re}} \text{ tangente: } y = 12(x - \underset{\substack{\uparrow \\ \text{point } 12}}{12}) + \underset{\substack{\uparrow \\ \text{en } (12; \dots)}}{f(12)}$$

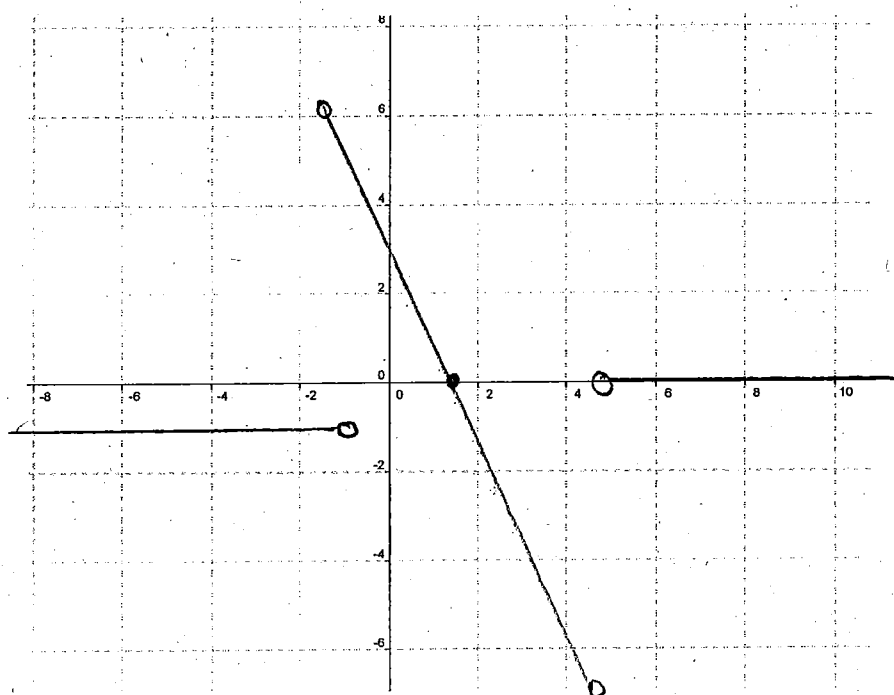
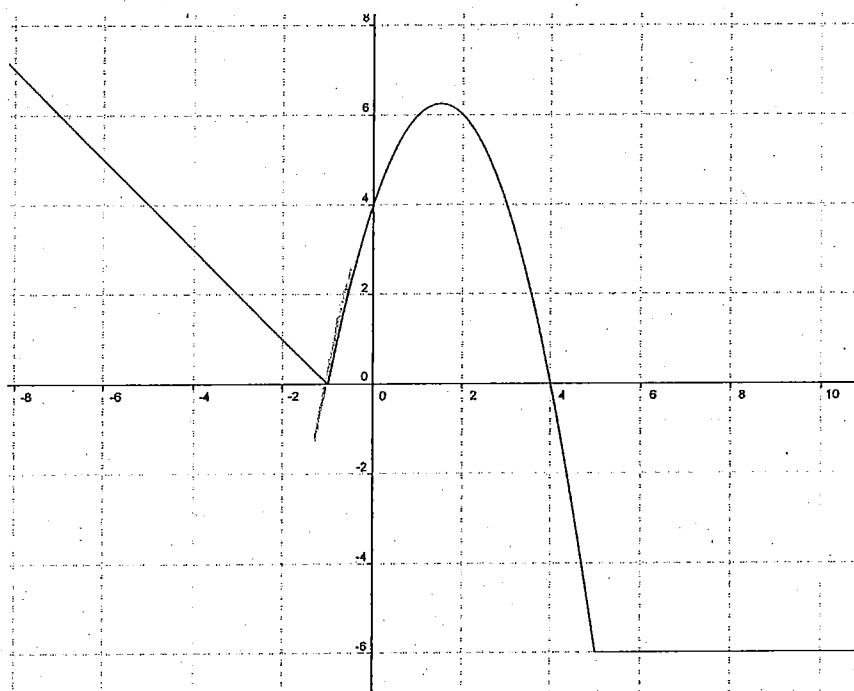
$$\Leftrightarrow y = 12x - 144 + 579 = 12x + 435$$

$$2^{\text{e}} \text{ tg: } y = 12(x - (-2)) + f(-2)$$

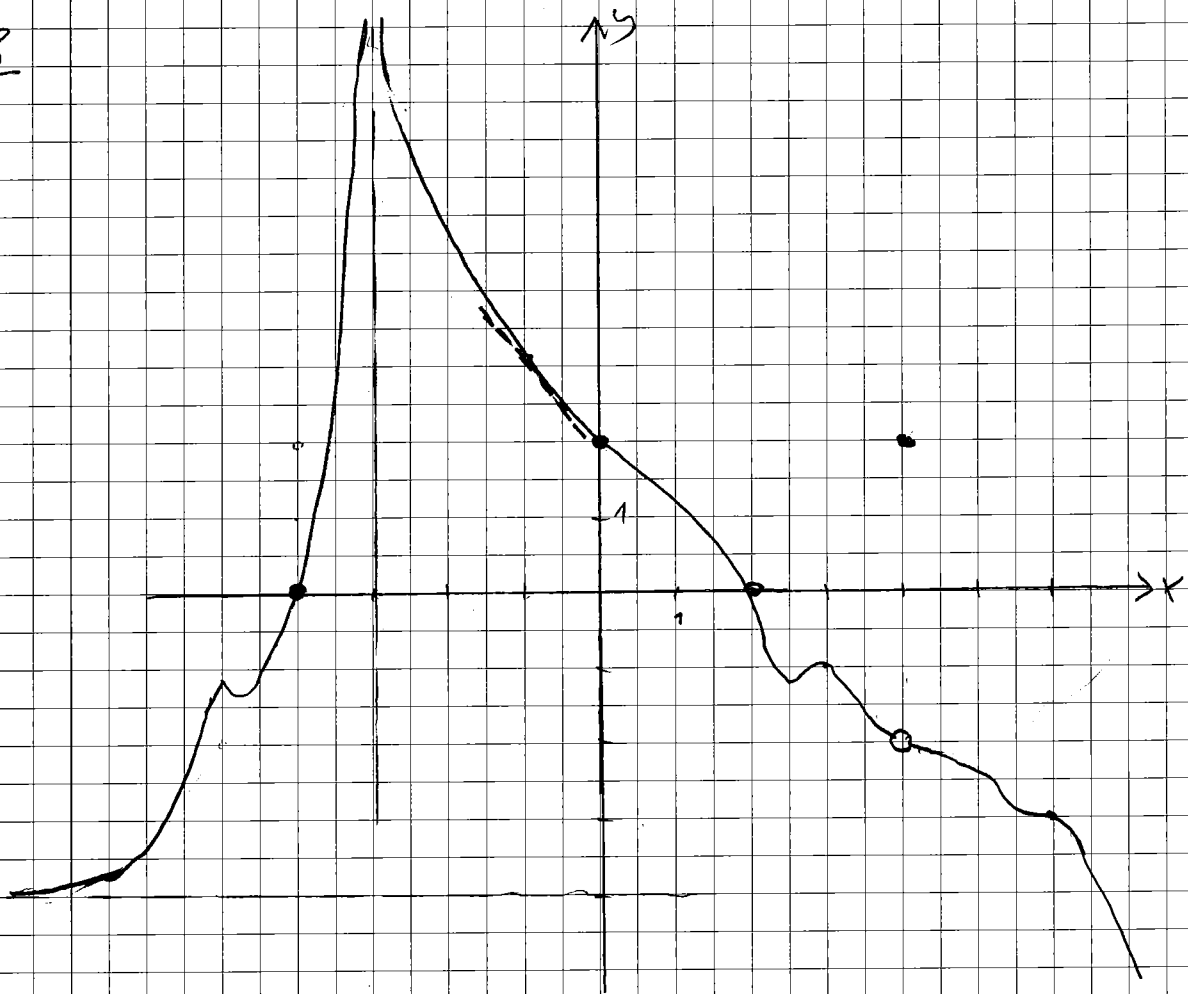
$$\Leftrightarrow y = 12x + 24 + 103 = 12x + 127$$

Exercice 9

On donne ci-dessous une représentation graphique d'une fonction réelle f . Tracer soigneusement une esquisse d'une représentation graphique de la fonction dérivée f' de f dans le repère supplémentaire fourni en-dessous :



ex 8



ex 10

(a) $\lim_{x \rightarrow -4^+} f(x) = +\infty$

(f) ~~?~~

(b) ~~?~~

(g) $+\infty$

(c) ~~?~~

(h) $-\infty$

(d) 2

(i) $+\infty$

(e) ~~?~~

(j) $+\infty$

(k) -3

ex 11

$$x+y=60 \Leftrightarrow y=60-x$$

$xy^3 \rightarrow \text{opt}$

$$f(x) = x(60-x) = 60x - x^2$$

$$f'(x) = 60 - 2x$$

x	0	30	60
f'(x)	+	0	-
f(x)		max	

les 2 robes sont
positif, donc
 $x \in [0; 60]$

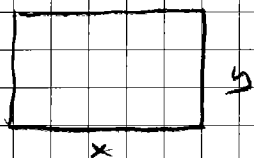
(a) $x=30$ et $y=30$: max pour 30 et 30

(b) on teste "les bords" : $x=0$ et $y=60$: $xy^3=0$

$x=60$ et $y=0$: $xy^3=0$

$\Rightarrow$ min pour 0 et 0

ex 12



$$2x+2y=30 \Leftrightarrow y = \frac{30-2x}{2} = 15-x$$

$$A = xy = x(15-x) = 15x - x^2$$

$$A'(x) = 15 - 2x$$

x	7,5
A'(x)	0
A(x)	max

dimensions : $x=7,5 \text{ cm}$ et $y=7,5 \text{ cm}$
c'est le carré !

Ex 13

1^{er} H
(André)

$\frac{1}{6}$ /
donne avec
sa femme

$\frac{5}{6}$ /
ne donne pas
avec sa femme

(René) 2nd H

$\frac{1}{6}$ / $\frac{5}{6}$

$\frac{1}{6}$ / $\frac{5}{6}$

⋮

6th H

(a) $P(A) = \frac{1}{6} \cdot \frac{1}{6} \cdot \dots \cdot \frac{1}{6} = \left(\frac{1}{6}\right)^6 = \frac{1}{216}$

(b) $P(B) = \frac{1}{6}$

(c) $P(C) = \frac{1}{6} \cdot \frac{1}{6} = \frac{1}{36}$

(d) $P(D) = P(B) + P(C) - P(B \cap C) = \frac{1}{6} + \frac{1}{6} - \frac{1}{36} = \frac{6+6-1}{36} = \frac{11}{36}$

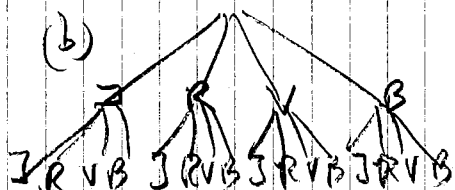
Ex 14 (a) i] $\Omega = \{J; R; V; B\}$ où J: "obtient une boule jaune"

$p(J) = \frac{8}{20}$ $p(R) = \frac{6}{20}$ $p(V) = \frac{4}{20}$ $p(B) = \frac{2}{20}$

ii] $p(\bar{J}) = 1 - \frac{8}{20} = 1 - \frac{2}{5} = \frac{3}{5}$

$p(R \cup V) = p(R \cup V) = p(R) + p(V) - p(R \cap V)$
 $= \frac{6}{20} + \frac{4}{20} = \frac{10}{20} = \frac{1}{2}$

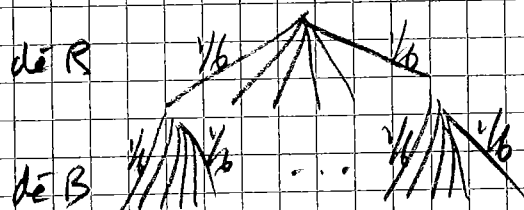
iii] $p(\bar{N}) = p(\Omega) = 1$



i] $p(JJ) = \frac{8}{20} \cdot \frac{7}{19} = \frac{14}{95}$

ii] $p(RV \cup VR)$
 $= \frac{6}{20} \cdot \frac{4}{19} + \frac{4}{20} \cdot \frac{6}{19} = \frac{12}{95}$

ex 15



(a) i] $p(A) = \frac{1}{6} \cdot \frac{1}{6} = \frac{1}{36}$

ii] $p(B) = p(\text{"14" ou "41"}) = 2 \cdot \frac{1}{6} \cdot \frac{1}{6} = \frac{2}{36} = \frac{1}{18}$

iii] $p(C) = p(11 \cup 22 \cup \dots \cup 66) = 6 \cdot \frac{1}{36} = \frac{1}{6}$

iv] $p(D) = p(15 \cup 51 \cup 24 \cup 42 \cup 33) = 5 \cdot \frac{1}{36} = \frac{5}{36}$

v] $p(E) = 1 - p(\text{"aucun 6"}) = 1 - \frac{5}{6} \cdot \frac{5}{6} = 1 - \frac{25}{36} = \frac{11}{36}$

(b) $p(B \cup D) = p(B) + p(D) - p(B \cap D) = \frac{1}{18} + \frac{5}{36} - p(\emptyset) = \frac{7}{36}$

(c) $p(C \cup D) = p(C) + p(D) - p(C \cap D) = \frac{1}{6} + \frac{5}{36} - p(\text{"33"}) = \frac{11}{36} - \frac{1}{36} = \frac{5}{18}$

ex 16

a) $p(A) = \frac{6}{12}$

$p(B) = \frac{4}{12}$

$p(A \cap B) = p(\text{"6" ou "12"}) = \frac{2}{12}$

$$\left. \begin{array}{l} p(A) \cdot p(B) \neq p(A \cap B) \\ \Leftrightarrow \frac{6}{12} \cdot \frac{4}{12} \neq \frac{2}{12} \\ \Leftrightarrow \frac{1}{2} \cdot \frac{1}{3} \neq \frac{1}{6} \text{ ou:} \end{array} \right\}$$

$\Leftrightarrow$ indépendants

b) $p(A) = \frac{6}{13}$

$p(B) = \frac{4}{13}$

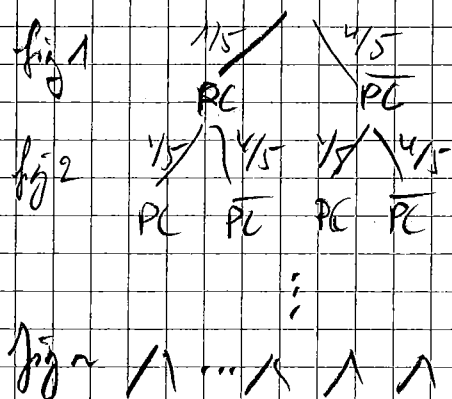
$p(A \cap B) = p(\text{"6" ou "12"}) = \frac{2}{13}$

$$\left. \begin{array}{l} p(A) \cdot p(B) \neq p(A \cap B) \\ \Leftrightarrow \frac{6}{13} \cdot \frac{4}{13} \neq \frac{2}{13} \end{array} \right\}$$

$\Leftrightarrow \frac{24}{169} \neq \frac{2}{13} \text{ non}$

$\Leftrightarrow$ dépendants

ex 17



(a) $A = \text{"au moins une fois PC"}$

$$P(A) \geq 80\%$$

$$\Leftrightarrow 1 - P(\text{aucune PC}) \geq 0,8$$

$$\Leftrightarrow 1 - \left(\frac{4}{5}\right)^n \geq 0,8$$

$$\Leftrightarrow \left(\frac{4}{5}\right)^n \leq 0,2$$

$$\Leftrightarrow \log\left(\left(\frac{4}{5}\right)^n\right) \leq \log(0,2)$$

$$\Leftrightarrow n \log\left(\frac{4}{5}\right) \leq \log(0,2)$$

$$\Leftrightarrow n \geq \frac{\log(0,2)}{\log(4/5)} \quad \downarrow \div \log(4/5) < 0$$

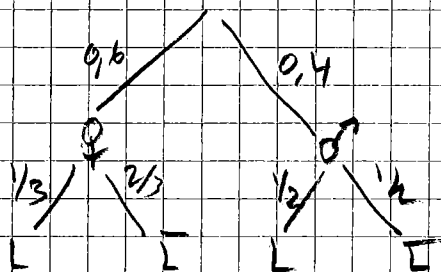
$$n \geq 7,21$$

Au moins 8 papuets

(b) idem avec $P(A) \geq 90\%$ $\Leftrightarrow \dots \Leftrightarrow n \geq \frac{\log 0,1}{\log 4/5} = 10,32$

au moins 11 papuets

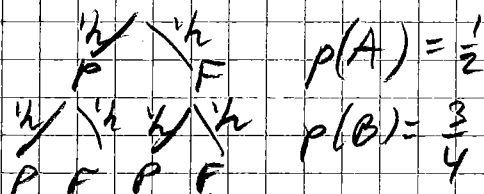
ex 18



$$P(\text{♀} | L) = \frac{P(\text{♀} \cap L)}{P(L)}$$

$$= \frac{0,6 \cdot \frac{1}{3}}{0,6 \cdot \frac{1}{3} + 0,4 \cdot \frac{1}{2}} = 0,5$$

ex 19



$$P(A) = \frac{1}{2}$$

$$P(B) = \frac{3}{4}$$

$$P(A \cap B) = P(\text{"PP"}) = \frac{1}{4}$$

$$P(A)P(B) \stackrel{?}{=} P(A \cap B) \Leftrightarrow \frac{1}{2} \cdot \frac{3}{4} \stackrel{?}{=} \frac{1}{4} \quad \text{non}$$

$\Rightarrow$ dépendants

ex 20

$$p(A) = \frac{4}{52}$$

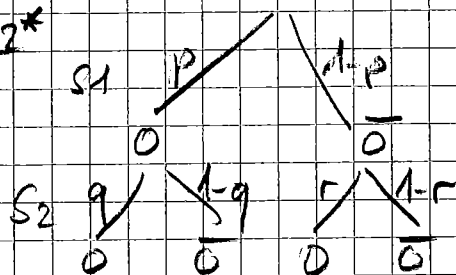
$$p(B) = \frac{13}{52}$$

$$p(A \cap B) = \frac{1}{52}$$

$$\frac{4}{52} \cdot \frac{13}{52} \neq \frac{1}{52} \text{ ou } \Rightarrow \text{independent}$$

ex 21 $p(P) = \frac{1}{2}$

ex 22*



$$p(0 \text{ et } 0) = p \cdot q = 0,5 \quad (\text{I})$$

$$1 - p(\bar{0} \text{ et } \bar{0}) = 1 - (1-p)(1-r) = 0,9 \quad (\text{II})$$

$$\text{et on a: } p(S1 \text{ occ}) = p(S2 \text{ occ})$$

$$\Leftrightarrow p = pq + (1-p) \cdot r$$

$$\Leftrightarrow p = 0,5 + r - pr \quad (\text{III})$$

$$(\text{II}): 1 - [1 - p - r + pr] = 0,9$$

$$\Leftrightarrow p + r - pr = 0,9$$

$$\Leftrightarrow r - pr = 0,9 - p$$

$$\text{dans (III): } p = 0,5 + [0,9 - p]$$

$$2p = 0,14$$

$$p = 0,7$$

$$\Rightarrow \text{dans (III): } 0,7 = 0,5 + r - 0,7r$$

$$\Leftrightarrow 0,2 = 0,3r$$

$$\Leftrightarrow r = \frac{2}{3}$$

$$\text{dans (I): } q = \frac{0,5}{p} = \frac{5}{7}$$

$$(a) P(S1 \bar{0}) = 1 - p = 1 - 0,7 = 0,3$$

$$(b) P(S1 \bar{0} \text{ et } S2 \bar{0}) = (1-p)(1-r)$$

$$= 0,3 \cdot (1 - \frac{2}{3}) = \frac{3}{10} \cdot \frac{1}{3} = \frac{1}{10} = 0,1$$

$$(c) 1 - P(S1 0 \text{ et } S2 0) = 1 - pq = 1 - 0,5 = 0,5$$

$$(d) P(S1 0 \text{ et } S2 \bar{0} \text{ ou } S1 \bar{0} \text{ et } S2 0) = p(1-q) + (1-p) \cdot r$$

$$= 0,7 \cdot \frac{2}{7} + 0,3 \cdot \frac{2}{3} = \frac{1}{5} + \frac{1}{5} = \frac{2}{5}$$

$$(e) P(S2 \bar{0} | S1 0) = 1 - q = \frac{2}{7}$$

$$(f) p(A) = p = 0,7$$

$$p(B) = pq + (1-p)r = 0,5 + 0,3 \cdot \frac{2}{3}$$

$$= 0,7$$

$$p(A \cap B) = pq = 0,5$$

$$0,7 \cdot 0,7 \neq 0,5 \text{ mm}$$

$\Rightarrow$ dependants